# A Regulation-Free Sub-0.5-V 16-/24-MHz Crystal Oscillator With 14.2-nJ Startup Energy and 31.8-μW Steady-State Power

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Abstract—This paper reports a regulation-free sub-0.5-V crystal oscillator (XO). The XO specifically designed for Bluetooth low-energy (BLE) radios aims for direct-powering by the harvested energy. To secure its performance against process, voltage, and temperature (PVT) variations, while reducing its startup time and energy, we propose a dual-mode  $g_m$  scheme and a scalable self-reference chirp injection (SSCI) technique. The former employs an inductive multistage  $g_m$  to mitigate the crystal's stray capacitance during the startup, but a single-stage  $g_m$  in the steady state to preserve the phase noise (PN). For the latter (SSCI), we generate a scalable chirping sequence to kickstart the XO, avoiding trimming of the auxiliary oscillator. The XO fabricated in 65-nm CMOS is measured with two common crystals (16/24 MHz) over a 0.3-to-0.5-V supply. At 24 MHz and 0.35 V, the startup time and energy of the XO are 400  $\mu$ s and 14.2 nJ, respectively, while showing a steady-state power of 31.8 µW and a PN of -134 dBc/Hz at 1-kHz offset. The frequency stability is 14.1 ppm against temperature (-40 °C-90 °C) and 17.9 ppm against voltage (0.3-0.5 V), both conform to the BLE standard ( $\pm 50$  ppm) with adequate margin.

*Index Terms*—Bluetooth low-energy (BLE), chirping, CMOS, crystal oscillator (XO), duty-cycling, energy harvesting (EH), fast startup, Internet-of-Things (IoT), ultralow power (ULP), ultralow voltage (ULV).

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10 1280 Es Percentage of ETOTAL Etrx (nJ) PTRX (mW) 000 30% ×0% 50% ~60% -70% 80% 0.1 12.8 10 100 1000 Es (nJ)

Fig. 1. Percentage of energy consumed during the startup of the XO over the total energy  $E_{\text{TOTAL}} = P_{\text{TRX}} \times T_{\text{ON}} + P_{\text{SLEEP}} \times T_{\text{OFF}} + E_S$ .  $P_{\text{SLEEP}}$ (assumed 1  $\mu$ W here, as approximated from [7]) is the sleep power,  $T_{\text{ON}}$ (128  $\mu$ s) and  $T_{\text{OFF}}$  (128 ms) are the assumed active time and sleep time of the TRX, respectively.

## I. INTRODUCTION

LTRALOW-POWER (ULP) wireless radios are the cornerstone of a wide variety of Internet-of-Things (IoT) applications. In particular, for the environmental monitoring, the ULP radios should operate under intermittent operation [1] to further reduce the data handling while prolonging the battery lifetime. Each ULP radio requires a stable reference for frequency synthesis at RF. The crystal oscillator (XO) is a reliable solution, but without the startup aid, it can take a few milliseconds for the XO to settle into the steady state [2]-[5] due to the high quality factor of the crystal  $(\sim 10^5)$ . Its startup time  $(t_s)$  dominates the "ON" latency of the radio, and its startup energy  $(E_S)$  can significantly degrade the effectiveness of duty cycling. As depicted in Fig. 1, if the active energy  $(E_{\text{TRX}})$  of a transceiver (TRX) is 1280 nJ (ON-time of 128  $\mu$ s [6] and active power of 10 mW [7]), the percentage of energy spent for starting the XO in every working cycle is  $\sim 42\%$  for  $E_S$  of 1000 nJ for conventional XO and a duty cycle of 0.1%. Such a percentage is going up since recent TRXs have managed to lower their active power  $(P_{\text{TRX}})$  by proper circuit techniques [8]–[10]. In this regard, it is essential to reduce  $E_S$  for the ULP radios to save energy by duty cycling. Recent efforts in both academia

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Fig. 2. Estimated lifetime of a commercial coin battery AG4 versus  $P_{\text{TRX}}$ , which can be expressed as: battery capacity/( $P_{\text{TRX}} \times$  active duty cycle).

and industry succeeded in shortening  $t_s$  and  $E_s$  of the XO [6], [7], [11]–[16].

On the other hand, long-term sustainability of wireless sensor nodes is another critical perspective of IoT deployment. For battery-powered ULP radios, the effort of battery replacement is largely labor-intensive. Even with a 0.1% active cycle, and a  $P_{\text{TRX}}$  of 2.3 mW, the lifetime of a ULP radio can hardly exceed a year under a coin-size battery (Fig. 2). For the prospect of one trillion IoT devices in the years to come, it implies 2.7 billion of batteries replacement daily, being a tremendous effort and unsustainable to the environment. To this end, energy harvesting (EH) offers the outlook for perpetual operation [17]–[19] of the ULP radios, while eliminating the cost and volume limit of the battery. Thermoelectric (10–1000  $\mu$ W/cm<sup>2</sup>) and photovoltaic (indoor: 10–100  $\mu$ W/cm<sup>2</sup>) are promising ambient sources, but their sub-0.5-V outputs [17] are too low for typical circuit solutions, and can vary (although slowly) with the environmental factors (e.g., temperature or light intensity). These facts motivate a new paradigm of analog and RF circuits that can survive against an inconstant sub-0.5-V supply voltage ( $V_{DD}$ ), eliminating the cost and loss of interim dc-dc converters and regulators.

This paper reports a regulation-free sub-0.5-V XO according to the system aspect of the EH Bluetooth low-energy (BLE) radios described in [20]–[23]. Unlike the existing fast-startup XOs that are based on standard or I/O voltages to powerup their inverter-like or active-load amplifiers [6], [11]–[14], our proposed XO is ultralow-voltage (ULV)-enabled by using single-/multistage resistive-load amplifiers. This circumvents from the ineluctable voltage headroom limit, rendering it compatible with the ULV application. Specifically, we propose a dual-mode  $g_m$  scheme and a scalable self-reference chirp injection (SSCI) technique for the XO to surmount the operating challenges in both startup and steady state (Fig. 3). The reported XO includes load capacitors of 6 pF and suits common commercially available crystals. Yet the technique can also be applied to crystals with different load capacitances.



Fig. 3. Overview of the proposed XO and illustration of  $t_S$  improvement by two techniques: SSCI and inductive three-stage  $g_m$ .  $L_M$ ,  $C_M$ , and  $R_M$  are the modeled inductance, capacitance, and resistance of the crystal, respectively, whereas  $C_S$  is the crystal's stray capacitance.

This paper is expanded from [24], with additional details and measurement results.

After the introduction, Section II details the proposed dualmode  $g_m$  scheme and SSCI. Section III presents the transistorlevel design of the sub-0.5-V XO. Section IV summarizes the experimental results, and finally, Section V draws conclusions.

# II. FAST-STARTUP XO USING DUAL-MODE $G_m$ SCHEME AND SSCI

For a crystal's resonant frequency  $(f_m)$  at tens of megahertz, its  $t_s$  (milliseconds) dominates the "ON" latency of a dutycycled radio, raising the average power consumption. As well, for energy-limited EH sources, the startup energy  $(E_s)$  of the XO is crucial as it may demand a large instant current from the EH source or reservoir. Recent XOs [6], [11]–[15] have succeeded in reducing both  $t_s$  and  $E_s$ . Herein, we propose two techniques: dual-mode  $g_m$  and SSCI, for balancing the XO performances in both startup (i.e.,  $t_s$  and  $E_s$ ) and steady state [i.e., power consumption and phase noise (PN)]. The envelope of the XO during the startup at time t is

$$A_{\rm env}(t) = A_i \cdot e^{\frac{R_N - R_M}{2L_M}t}$$
(1)

where  $A_i$  is the initial amplitude and  $R_N$  is the negative resistance of the overall impedance viewed from the crystal core (details in Section II-B).  $L_M$  and  $R_M$  are the motional inductance and resistance of the crystal, respectively. The aim of SSCI is to increase  $A_i$  instantly after enabling the XO, while the dual-mode  $g_m$  allows a boosted  $R_N$  afterward. They together bring down  $t_S$  without momentarily raising the startup power, culminating in a lower  $E_S$  and a relaxed power-source design, with details presented in the following.

## A. Scalable Self-Reference Chirp Injection

Signal injection to the XO can bring down  $t_s$  if the injection frequency is close to  $f_m$  of the crystal [12]. Instead of waiting for the XO to build up its oscillation amplitude, an auxiliary oscillator (AO) can be used to excite the crystal. Yet, due to the high-Q nature of the crystal, such signal injection is only



Fig. 4. General illustration of different signal-injection techniques in the frequency domain. Assuming the total power of each injection signal is similar, the crystal absorbs more power from CFI than CI since the CI spectrum spreads over a broader band.

effective if its frequency does not deviate by >0.5% from  $f_m$  [6]. Several signal-injection techniques for kick-starting the XO have been reported. They can be categorized into three groups: constant frequency injection (CFI) [11], [14], [15], dithering injection [6], and chirp injection (CI) [12].

CFI injects a clock signal into the crystal with a constant frequency close to  $f_m$ , as illustrated in the frequency domain (Fig. 4). With a constant frequency and narrow bandwidth (e.g., full-width at half-maximum of the 7.7- $\mu$ s pulse in [14]: 156 kHz), a clock frequency precisely matching  $f_m$  is essential to excite the crystal. This involves calibration as well as a delicate design for the AO which will be challenging in a sub-0.5-V design. As an example, the XO in [14] achieves  $t_s$  values of 58/10/2  $\mu$ s from 1.84/10/50 MHz crystals. Yet it has a supply voltage of 1 V. Also, the ring oscillator entails frequency calibration after fabrication.

Dithering injection toggles the AO frequencies between two values by compensating the frequency deviation of the injection signal caused by temperature and voltage variations. As such, the injection signal can cover a wider frequency range than that of CFI. Still, trimming is necessary to compensate the process variation on the AO. Compared with CFI, its effect on shortening  $t_s$  is lower, since the signal power is spread to a wider spectrum. As a result, there is smaller power to be absorbed by the crystal at  $f_m$ . For instance, the XO in [6] exhibits a slashed  $t_s$  of <400  $\mu$ s by using dithered-signal injection (dithered step size: 2%), but it still demands trimming to manage the process variations on the injection oscillator.

Here, we consider CI to be more robust and inexpensive, as it relies on a frequency-rich signal to excite the crystal and avoids frequency calibration. The principle is alike dithering but covers a wider frequency range. It gradually sweeps the oscillating frequency and progressively decreases/increases the frequency. As such, this chirping sequence can generate a spectrum between the highest frequency  $f_H$  and the lowest frequency  $f_L$ , as evinced by its Fourier transform [25]. If  $f_L < f_m < f_H$  regardless of process, voltage, and temperature (PVT) variations, the power will be delivered to the crystal persistently. Despite its weaker effectiveness on  $t_S$  reduction since the power spreads to a wider band, CI has the benefit of no trimming on the AO. It is especially suitable for low-cost and ULV radios, where the frequency variation of the AO against voltage and temperature can be more exacerbated.

TABLE I Overview of Different Signal-Injection Techniques to Kick-Start the XO

	Characteristics of the injecting signal							
	Constant frequency	Dithering	Chirping					
ts & Es reduction	~~~	$\checkmark\checkmark$	✓					
Trimming on AO	Required	Required	Not required					
Precision of AO	Very critical	Critical	Relaxed					
Literature	[14, 15]	[6]	[12] and this work					



Fig. 5. Proposed SSCI. It generates a chirping signal to kick-start the XO using an untrimmed RO with relaxed precision. The FSM provides feasibility to scale  $t_{CI}$ , accommodating different crystal packages (i.e.,  $L_M$  and  $C_S$ ).

In [12], CI was applied together with the  $R_N$ -boosting technique, showing a  $t_S$  of 158  $\mu$ s without trimming or calibration on the AO. Still, the related *RC*-sweeping unit for modulating the frequency of the AO is area hungry (estimated ~90% of the chip area) due to its large time constant (at the order of 10  $\mu$ s) for generating the chirping sequence. Table I summarizes the key features of the three signal-injection techniques.

To avoid the pitfalls of [12], we introduce the SSCI (Fig. 5) that only entails an untrimmed oscillator with relaxed precision. Its frequency range can easily cover  $f_m$  variation against PVT. Unlike the *RC*-based chirping [12], here we incorporate a five-stage RO with a finite state machine (FSM) to control the oscillating frequency of the RO via a cap-bank. Hence, the chirping sequence can be generated by referencing its own signal and requiring no area-hungry *RC*-units to modulate the oscillating frequency. The FSM counts the number of pulses and sequentially raises  $C_{OSC}$  by sending the control signal  $f_{ctrl}$  to the RO. In addition, compared to the analog sweeping technique in [12], the FSM can digitally scale the total injection time ( $t_{CI}$ ), decided by the number of exciting cycles at each cap-bank value  $C_{OSC}$ 

$$t_{\rm CI} = N \times \sum_{i} t_i \tag{2}$$

where N is the number of cycles to repeat at each  $C_{OSC}$ , and  $t_i$  is the period of a single cycle at *i*th  $C_{OSC}$ . The average amplitude of oscillation on the crystal after the chirping sequence is proportional to  $\sqrt{t_{CI}}$ , as suggested from the Fourier transform of the chirping sequence [25] and also the time-domain



Fig. 6. XO using (a) one-single  $g_m$  ( $A_{XO-1}$ ) for the steady-state and (b) three-stage  $g_m$  ( $A_{XO-3}$ ) for the startup.

analysis in [12]. Thus, N can be programmed to adjust  $t_{CI}$ , rendering the XO easily compatible with different crystal parameters, i.e., an optimum  $t_{CI}$  depends on  $L_M$ ,  $R_M$  and  $R_N$  ( $C_S$ ) [12]. This digital-intensive architecture is more area efficient. The oscillation signal at the RO has varying duty-cycle with VT-variation. To maximize the injection energy (i.e., 50% duty cycle), the chirp-modulated signal is a div-by-2 output of the RO. This output serves as both the exciting signal for the crystal via the output driver, and the trigger signal for the FSM. The RO is powered down by the FSM automatically after the injection.

# B. Dual-Mode $g_m$ Scheme

The XO using a one-stage  $g_m$  ( $A_{XO-1}$ ), especially for the Pierce oscillator, is popular as it can optimize the steady-state PN [6], [12]–[14], [26]. The  $g_m$  offers a negative resistance compensating the equivalent resistance of the crystal. Its value also determines the growth of the oscillation amplitude before the XO reaches the steady state. As shown in Fig. 6(a), by omitting the resistive loss induced by  $A_{XO-1}$ , the impedance between the I/O ( $Z_{amp-1}$ ) becomes

$$Z_{\rm amp-1} = -\frac{g_m}{4\omega_0^2 C_L^2} + \frac{1}{j\omega_0 C_L}$$
(3)

where  $C_L$  is the designated crystal's load capacitance and  $\omega_0$  is the angular oscillating frequency  $2\pi f_0$ . Since  $Z_{amp}$  is shunted by the crystal's stray capacitance ( $C_S$ ), the negative resistance ( $R_N$ ) of the overall impedance looking from the crystal core ( $Z_C$ ) is affected

$$R_N \equiv -\operatorname{Re}(Z_c) = \frac{-\operatorname{Re}(Z_{\text{amp}})}{[\omega_0 C_s \operatorname{Re}(Z_{\text{amp}})]^2 + [1 - \omega_0 C_s \operatorname{Im}(Z_{\text{amp}})]^2}.$$
(4)

If  $\omega_0 C_S |Z_{amp}| \ll 1$ , we can have  $R_N \approx -\text{Re}(Z_{amp})$  that matches the expression in [6] for  $A_{XO-1}$ . A large  $R_N$  favors more  $t_S$  reduction according to (1). Yet, for  $|Z_{amp}|$  to be comparable with  $1/\omega_0 C_S$  [i.e., a higher  $g_m$  and thus  $|\text{Re}(Z_{amp})|$ to speed up the startup], we have to cogitate the effect from  $C_S$ . Thus, we can deduce the specific  $R_N$  of  $A_{XO-1}$  (i.e.,  $R_{N,1}$ ) from (4) as given by

$$R_{N,1} = \frac{4g_m C_L^2}{(g_m C_s)^2 + 16C_L^2 \omega_0^2 (C_L + C_S)^2}.$$
 (5)



Fig. 7. Plot of the impedances as function of  $C_{o1}$  and  $C_{o2}$ . (a) Re( $Z_{amp-3}$ ). (b) Im( $Z_{amp-3}$ ). (c) Re( $Z_{C-3}$ ). (d) Im( $Z_{C-3}$ ). For (a) and (b), the contours where Re( $Z_{amp-3}$ ) = 0 k $\Omega$  and Im( $Z_{amp-3}$ ) = 0 k $\Omega$  are depicted with red lines.

Taking the derivative of (5), we can obtain the maximum value of  $R_{N,1}$  with respect to  $g_m$  at a fixed  $C_L$ 

$$R_{N,1,\max} = \frac{C_L}{2\omega_0 C_s (C_L + C_s)} \tag{6}$$

where we apply  $g_m = 4\omega_0 C_L(1 + C_L/C_s)$ . Obviously, Im( $Z_{amp-1}$ ) can only be negative (capacitive) for  $A_{XO-1}$ , and  $R_{N,1}$  has an upper limit if only  $g_m$  is the sizing parameter [12], [13]. For instance,  $R_{N,1}$  is limited to 1.2 k $\Omega$  with  $C_S = 2$  pF,  $f_0 = 24$  MHz, and  $C_L = 6$  pF, even if we apply an oversized  $g_m = 14.5$  mS. There were efforts to raise  $R_{N,1}$  by increasing  $g_m$  or tuning  $C_L$  temporarily during the startup [13], [26], [27]. Yet, increasing  $g_m$  incurs in larger power consumption and is unfavorable toward reduction of  $E_S$ . Furthermore,  $R_{N,1}$  is bound by (6), and is maximally  $1/2\omega_0 C_S$ (i.e., 1.66 k $\Omega$  in the above example when  $C_L \gg C_S$  and  $g_m \approx 4\omega_0 C_L^2/C_S$ ).

Inspecting (4), if a positive  $\text{Im}(Z_{\text{amp}})$  is possible to counteract the effect of  $C_S$ ,  $R_N$  can be boosted to surmount the aforesaid  $R_N$ -limit. Our idea is to mimic a microhenry-range inductor on chip for this purpose. Interestingly, it is found that a three-stage  $g_m$  ( $A_{\text{XO}-3}$ ) with designated capacitive loads ( $Z_{o1-2}$ ) can effectively mimic an inductive effect during the startup [Fig. 6(b)]. Although a multistage  $g_m$  has been applied in [28] to save the XO's steady-state power, this paper explores first its inductive feature for  $t_S$  reduction. For  $A_{\text{XO}-3}$ , we define its  $Z_{\text{amp}}$  as  $Z_{\text{amp}-3}$  as given by

 $Z_{amp-3}$ 

$$= \frac{-G_{m,\text{eff}}}{4\omega_0^2 C_L^2 (1 + j\omega_0 r_{o1} C_{o1})(1 + j\omega_0 r_{o2} C_{o2})} + \frac{1}{j\omega_0 C_L}$$

$$= -\frac{G_{m,\text{eff}} (1 - \omega_0^2 r_{o1} C_{o1} r_{o2} C_{o2})}{4\omega_0^2 C_L^2 [1 + (\omega_0 r_{o1} C_{o1})^2] [1 + (\omega_0 r_{o2} C_{o2})^2]}$$

$$+ \frac{1}{j\omega_0 C_L} \left\{ 1 - \frac{G_{m,\text{eff}} (r_{o1} C_{o1} + r_{o2} C_{o2})}{4C_L [1 + (\omega_0 r_{o1} C_{o1})^2] [1 + (\omega_0 r_{o2} C_{o2})^2]} \right\}$$
(7)

where  $G_{m,\text{eff}} = g_{m1} \cdot r_{o1} \cdot g_{m2} \cdot r_{o2} \cdot g_{m3}$  and  $Z_{o1/2}$  is represented as a parallel load of  $r_{o1/2}$  and  $C_{o1/2}$ . Since at 24 MHz the impedance of  $2C_L$  at the output (553  $\Omega$ ) is usually much smaller than the resistive load of the third stage, its resistive part is neglected. Manifested from (7), both the real and imaginary parts of  $Z_{\text{amp}-3}$  are unbounded between positive and negative. For a positive Im( $Z_{\text{amp}-3}$ ), (8) has to be satisfied

$$\frac{G_{m,\text{eff}}(r_{o1}C_{o1} + r_{o2}C_{o2})}{[1 + (\omega_0 r_{o1}C_{o1})^2][1 + (\omega_0 r_{o2}C_{o2})^2]} > 4C_L.$$
 (8)

Alternatively, for a negative  $\text{Re}(Z_{\text{amp}-3})$ , we set  $1/(r_{o1,2}C_{o1,2}) > \omega_0$ . In a practical design, the complete independent variables are only  $C_{o1,2}$  and  $g_{m1,2,3}$  as  $r_{o1,2}$  are correlated with  $g_{m1,2}$ , especially when the voltage headroom is restrained. Fig. 7(a) and (b) plots  $\text{Re}(Z_{\text{amp}-3})$  and  $\text{Im}(Z_{\text{amp}-3})$ , as a function of  $C_{o1,2}$ , respectively, where we set  $g_{m1,2} = 0.4$  mS,  $g_{m,3} = 1.5$  mS,  $r_{o1,2} = 7$  k $\Omega$ ,  $C_L = 6$  pF, and  $\omega_0 = 2\pi \times 24$  MHz. At small  $C_{o1,2}$ , we have  $\text{Re}(Z_{\text{amp}-3}) = -G_{m,\text{eff}}/4\omega_0^2 C_L^2$ .  $\text{Re}(Z_{\text{amp}-3})$  increases to 0 k $\Omega$  when we enlarge  $C_{o1,2}$ , and turn to positive if  $C_{o1}C_{o2} > 1/\omega_0^2 r_{o1}r_{o2}$  [red line in Fig. 7(a)].

For Im( $Z_{amp-3}$ ), it is negative (capacitive) for sufficient small or large  $C_{o1,2}$ , but can be turned to positive (inductive) within a specific range, defined by the quadratic equation in (8) and shown in Fig. 7(b). By solving (8), the desired inductive effect can be achieved. For example, for  $C_{o1} = C_{o2} = 0.5$  pF, the desirable inductive impedance  $Z_{amp-3} = -1.6 + 1.2$  j k $\Omega$ can be achieved.

Fig. 7(c) and (d) shows the changes of  $\text{Re}(Z_{C-3})$  and  $Im(Z_{C-3})$  after paralleling  $A_{XO-3}$ , respectively, with  $C_S = 2$ pF. When  $C_{o1}$  and  $C_{o2}$  are small, the value of  $\text{Re}(Z_{C-3})$  (i.e.,  $-R_{N,3}$ ) is alike to that of  $A_{XO-1}$  and is bounded by (5), in which  $g_m$  is replaced by  $G_{m,eff}$  that is  $\sim -1.2 \text{ k}\Omega$ . Such limitation can be surpassed here with an inductive  $Z_{amp-3}$  as derived in Fig. 7(b). For instance, for  $C_{o1} = C_{o2} = 0.5$  pF, we can have  $\operatorname{Re}(Z_{C-3}) = -2.4 \text{ k}\Omega$  due to the inductive  $A_{\rm XO-3}$ . Thus, a higher  $R_N$  can be achieved even with similar power consumption when compared to the  $A_{XO-1}$ , enabling an energy-efficient startup. Due to the intricate expression of  $R_{N,3}$ , its optimization is done numerically, as shown in Fig. 7(c), before proceeding to transistor- level implementation. Besides, our technique is also applicable to different  $f_0$ . Using a similar mathematical model derived by (4) and (7) and changing the total  $g_m$  and  $C_{o1,2}$  correspondingly, we have simulated to boost the  $R_N$  by 6.1× at  $f_0 = 10$  MHz and 7.4× at  $f_0 = 50$  MHz with the  $A_{XO-3}$  compared to  $A_{XO-1}$ . Since reference clock at 16/24 MHz is common for BLE as [6] and [13] reported, thus in this paper, we only focus on  $f_0 = 16$  and 24 MHz.

Apparently, for the same power budget,  $A_{XO-3}$  is inferior to  $A_{XO-1}$  in terms of the steady-state PN, as each stage shares a smaller bias current and the noises accumulate. Also, for Im( $Z_{C-3}$ ) that determines the exact oscillating frequency of the XO, it deviates from the designated value due to the presence of  $C_{o1}$  and  $C_{o2}$  [Fig. 7(d)]. This affects the accuracy of  $f_0$ . Thus, it is desirable to implement a dualmode  $g_m$  scheme that can balance the startup and steady-state performances. During the startup where the PN and accuracy



Fig. 8. Circuit implementation of (a)  $A_{XO-1}$  and (b)  $A_{XO-3}$ .

of  $f_0$  are irrelevant,  $A_{XO-3}$  is enabled and connected to the crystal to attain a larger  $R_N$  for fast startup. When the crystal has gained sufficient energy for oscillation,  $A_{XO-3}$  is OFF and disconnected from the crystal while  $A_{XO-1}$  takes over to sustain the oscillation. As a result, the XO can benefit from both  $A_{XO-3}$  (fast startup) and  $A_{XO-1}$  (low PN and accurate  $f_0$ ).

## **III. TRANSISTOR-LEVEL IMPLEMENTATION**

The core elements of the XO (e.g.,  $A_{XO-1}$ ,  $A_{XO-3}$ , and RO) are designed to operate below a 0.5-V  $V_{DD}$ . Only the static and dc circuits (digital logic and constant- $g_m$  bias circuit) operate at 0.7 V to facilitate the design. These circuits together consume <5  $\mu$ A and are mostly powered-off during the steady state. Thus, the 0.7-V supply can be easily generated by an on-chip switched-capacitor charge pump and shared with other blocks at the system level as described in [22].

Both  $A_{XO-1}$  and  $A_{XO-3}$  are based on subthreshold common-source (CS) amplifiers with resistive loads [Fig. 8(a) and (b)]. Unlike other solutions that use currentsource loads [6], [13], [14], the resistive load aids to preserve a moderate  $g_m$  even with  $V_{DD} < 0.35$  V, for a small bias current (simulated at  $I_{dc} = 100 \ \mu A$ ). For instance, the simulated  $g_m$ of  $A_{\rm XO-1}$  is 1.3 mS at  $V_{\rm DD} = 0.3$  V and -40 °C, being  $4 \times$  higher than that of the current-source load (assuming an identical  $g_m$  with  $V_{DD} = 0.35$  V at 20 °C). Furthermore, at high temperature, the intrinsic output resistance of the transistor decreases rapidly. This affects the stability of  $R_N$ and causes variation on  $t_s$ , especially for  $A_{XO-3}$ . The  $A_{XO-1}$ with resistive load has a tradeoff of lower immunity to power supply noise (noise power from  $V_{DD}$  modulated to the output of XO with a resistive load that is 3 dB larger than its current-source-load counterpart at 1-kHz offset). Also, it has a large  $f_0$  variation since the  $g_m$  of  $A_{XO-1}$  is not fixed. Still, this is manageable for the BLE standard ( $<\pm 50$  ppm [29]), as well as other IoT protocols (e.g., ZigBee: ±40 ppm). A small nominal  $I_{dc}$  of 100  $\mu$ A is adequate for the expected PN.

 $A_{\rm XO-1}$  is self-biased by a feedback resistor  $R_F$ , whereas  $A_{\rm XO-3}$  is an ac-coupled three-stage CS amplifier aided by a constant- $g_m$  bias circuit. As revealed by (7), the  $g_m$  of the  $A_{\rm XO-3}$  has a considerable impact on  $R_{N,3}$ . Thus, the constant- $g_m$  bias circuit secures  $A_{\rm XO-3}$  to be inductive, and a stable  $R_{N,3}$  for robust-and-fast startup against PVT. The channel lengths of the transistors are chosen such that their output resistances are  $\sim 10 \times$  larger than the resistors  $R_{1-3}$ .



Fig. 9. (a) Locus plot of the  $Z_{amp-1,-3}$  against frequency. (b) Simulated  $R_{N,1}$  and  $R_{N,3}$  with a fixed total  $g_m$  budget of 2.3 mS, and the boosting ratio against frequency.

This soothes temperature dependence of  $R_{N,3}$  as  $r_{o1-3}$  are then dominated by  $R_{1-3}$ . On the other hand, the widths of the transistors are deterministic of the parasitic capacitances. Especially for  $C_{GS}$  of the transistor, it not only is sensitive to the operating conditions and affects  $C_{o1,2}$  but also forms a capacitive divider with the ac-coupling network and degrades the gain; the gain attenuation should be controlled within 5% to depress their overall impacts.  $A_{XO-3}$  is designed to have similar power consumption (~100  $\mu$ A) as A<sub>XO-1</sub>. As such, the power consumption does not vary instantaneously, easing the design and layout of the power supply. CMOS switches are inserted to each current branch such that  $A_{XO-1}$  or  $A_{XO-3}$  can be isolated from the crystal while lowering their leakage power (simulated <14 nW at 0.35 V and 20 °C) when disabled. They have minimal channel lengths and adequate widths such that their ON-resistances are negligible when compared with  $R_{1-3}$ .

Both the parasitic capacitances of the transistors and the finite I/O resistance of  $A_{XO-3}$  will affect the accuracy of the derivation from (7). Thus,  $R_{N,3}$  should be further optimized via simulation. The total  $g_m$  budget is 2.3 mS (total bias current: 100  $\mu$ A, assuming a  $g_m/I_D = 23 \text{ V}^{-1}$ ), and  $r_{o1-3}$  are set according to the  $g_m$  of each gain stage. Fig. 9(a) shows the locus plots of  $Z_{amp-1}$  and  $Z_{amp-3}$  implemented with practical transistors and integrated passives.  $Z_{amp-1}$  is capacitive over all frequencies, while  $Z_{amp-3}$  is inductive over the 13-to-46-MHz range, rendering its compatible with different  $f_0$ . Optimized at the most popular XO frequency of 24 MHz, the optimum  $R_{N,3}$  is 2.4 k $\Omega$  after paralleling it with a  $C_S$  of 2 pF. This result is  $\sim 9 \times$  higher than  $R_{N,1}$  under the same  $g_m$ budget and surpasses  $R_{N,1,\text{max}}$  [Fig. 9(b)]. The boosting effect is insensitive to the frequency between 15 and 34 MHz, under  $R_{N,3}/R_{N,1} > 6.$ 

The Monte-Carlo-simulated  $R_{N,3}$  (mean) is >9.1× higher than  $R_{N,1}$ , and the boosting factor is immune to  $C_s = 1-3$  pF, as specified from the crystal manufacturer (Fig. 10). We design  $R_{N,1}$  to be >50  $\Omega$  against PVT to compensate the resistive loss of the crystal (measured  $R_M$  of the crystal: 19  $\Omega$ ), and safeguard the oscillation as well as PN of the XO.

Ideally,  $A_{XO-3}$  should be enabled for the entire startup phase. Yet the  $g_m$  values of  $M_{1-3}$  deviate from their smallsignal values when the oscillation amplitude is growing. This results in an aggravated  $R_{N,3}$ . Thus, the optimum active time of  $A_{XO-3}t_{sw}$  is the time when  $R_{N,3} \approx R_{N,1}$ , which means



Fig. 10. Monte-Carlo-simulated  $R_N$  ( $f_0 = 24$  MHz, N = 300,  $V_{DD} = 0.35$  V).



Fig. 11. (a) Monte-Carlo-simulated  $f_L$  with  $V_{\rm DD} = 0.4$  V and T = 90 °C. (b) Monte-Carlo-simulated  $f_H$  with  $V_{\rm DD} = 0.3$  V and T = -40 °C. N = 30 for both cases.

 $A_{\rm XO-3}$  no longer helps  $t_s$  reduction. The optimal  $t_{\rm sw}$  can be found via simulations with measured crystal parameters to avoid any extra detection and control mechanism.

To realize the SSCI, a five-stage RO is constituted by CS-amplifiers with source degeneration. Compared with the RO with inverters or relaxation oscillator, an RO with CS-amplifiers balances between the frequency stability and compatibility with the sub-0.5-V  $V_{DD}$ . The source resistor ( $R_S$  in Fig. 5) also reduces the variation of oscillating frequency against  $V_{DD}$ . From the simulation, the frequency variation of RO is reduced by ~20% over a 0.3-to-0.5 V  $V_{DD}$ .  $R_D$  is set to 36 k $\Omega$ . The current consumption of the RO is 20  $\mu$ A. We implemented the div-by-2 unit and FSM with a standard logic.

We designed the  $f_H$  and  $f_L$  of the SSCI module as 36 and 12 MHz, respectively, which are chosen such that  $f_L < f_m < f_H$  is satisfied even with PVT variation (Fig. 11). The total size of the  $C_{OSC}$  is simulated to be 135 fF to output an  $f_L$ of 12 MHz (after div-by-2). Then, the resolution of the capbank should be determined. This is decided by the minimum duration of  $t_{CI}$ ; since for a complete chirping sequence all of the states need to be swept at least once, the minimum  $t_{CI}$  (i.e., N = 1) is set by the resolution (number of pulses), as depicted in (2). The optimum  $t_{CI}$ , according to [12] and the measured crystal parameter, is derived as 4.6  $\mu$ s. Thus, we set  $C_{OSC}$  as a binary-coded 6-bit cap-bank (unit cap: 2.14 fF), corresponding to a minimum  $t_{CI}$  of 4  $\mu$ s with the designate



Fig. 12. Increase in  $t_s$  caused by the deviation of  $t_{CI}$  from the optimum duration.



Fig. 13. (a) Chip micrograph. (b) Area breakdown of the XO.

 $f_H$  and  $f_L$ . Even though there is a discrepancy between the applied and optimum  $t_{CI}$ , the  $t_s$  is almost unaffected as the  $t_{CI}$  is only present for a short period when compared with  $t_s$ . As manifested in Section II-A, the amplitude of oscillation after the CI is proportional to  $\sqrt{t_{CI}}$ . Thus, even the applied  $t_{CI}$  is 13% shorter than the optimum in our case, the amplitude is only 7% smaller. Thanks to the high growth of the oscillation amplitude of the  $A_{XO-3}$  [time constant in (1): 9.33  $\mu$ s], the discrepancy between the applied and optimum  $t_{CI}$  can be compensated by the  $A_{XO-3}$  quickly, e.g., the 0.6  $\mu$ s discrepancy is countervailed by the growth of oscillation amplitude in that 0.6  $\mu$ s (~1.07×). No significant difference on  $t_s$  will emerge, even with PVT variation on the  $t_{CI}$  (Fig. 12).

The RO generates an oscillating signal at  $2f_H$  with  $C_{OSC} = 0$  fF (with oscillating frequency governed by the parasitic capacitances), and  $C_{OSC}$  is progressively increased by the FSM bit-by-bit according to N to  $C_{OSC} = 135$  fF whereas the RO oscillates at  $2f_L$ . In this paper, the variable N is digitally configurable among 1, 2, 4, and 8.

#### **IV. EXPERIMENTAL RESULTS**

The XO was fabricated in 65-nm CMOS with fixed onchip  $C_L$  of 6 pF. Extra cap-bank can be added to the XO for finer control of  $C_L$  if necessary. The active area is 0.023 mm<sup>2</sup> [Fig. 13(a)], of which 36% corresponds to the load capacitors [Fig. 13(b)]. The target  $f_0$  can be flexible between 16 and 24 MHz. The FSM (i.e.,  $t_{CI}$ ) as well as the enabling of the  $V_{DD}$ are governed by a field-programmable-gate-array (Fig. 14). We first verify the SSCI functionality. Fig. 15(a) shows the measurement of the oscillating frequency of the RO (after divby-2) against  $C_{OSC}$ , which is consistent with the post-layout simulation. The frequency range of the chirping sequence can safely cover the designated  $f_m$  against voltage and temperature variations. The average  $f_L$  and  $f_H$  across five dies at room



Fig. 14. Measurement setup of the XO.



Fig. 15. (a) Measured and simulated oscillating frequencies of the RO versus  $C_{\text{OSC}}$  at different conditions, robust to cover  $f_0$  of the crystal even with  $V_{\text{DD}}$  and temperature variations. (b) Measured chirping sequence (N = 1). (c) Injection duration  $t_{\text{CI}}$  against N. For the latter two figures,  $V_{\text{DD}} = 0.35$  V, T = 20 °C.

temperature are 10.93 ( $\sigma$ : 0.32 MHz) and 35.96 MHz ( $\sigma$ : 1.21 MHz), respectively. Fig. 15(b) confirms the chirping sequence with N = 1 and Fig. 15(c) shows the duration of  $t_{\text{CI}}$  against N. This implies that the SSCI can generate a chirping sequence with variable  $t_{\text{CI}}$  (4–32  $\mu$ s in this paper) to accommodate different crystal parameters without resorting from area-hungry *RC*-units.

The XO was then tested with a 24-MHz crystal (package:  $3.2 \times 2.5 \text{ mm}^2$ ) without any startup aid at room temperature (20 °C) and  $V_{\text{DD}} = 0.35$  V. The measured crystal parameters  $L_M$ ,  $R_M$ ,  $C_M$ , and  $C_S$  are 11.1 mH, 19  $\Omega$ , 3.95 fF, and 1.3 pF, respectively. Under these conditions, we have  $t_s = 1.3$  ms [Fig. 16(a)].  $t_s$  is shortened to 530  $\mu$ s when  $A_{\text{XO}-3}$  is enabled during the startup.

Since directly measuring  $R_N$  by inserting a resistance in series with the crystal is not viable ( $R_N$  is the real part of the impedance seen by the crystal core, which cannot be separated from the  $C_S$ ), we have to estimate  $R_{N,1}$  and  $R_{N,3}$  from the growth of the oscillation amplitude according to (1), which can be rewritten as

$$\ln\left(\frac{A_{\rm env}(t_0 + \Delta t)}{A_{\rm env}(t_0)}\right) = \frac{R_N - R_M}{2L_M} \cdot \Delta t \tag{9}$$



Fig. 16. Measured startup waveform (a) without startup aid and (b) with SSCI and  $A_{XO-3}$  enabled.

where  $t_0$  is the starting time and  $\Delta t$  is the elapsed time. Hence, by measuring the growth of the oscillation amplitude within a specific time interval, the  $R_N$  of the XO can be estimated. For  $A_{\rm XO-1}$ , the growth of oscillation is  $1.01 \times / \mu$ s, and therefore  $R_{N,1}$  is calculated as 230  $\Omega$  (Fig. 17), which is close to the prediction as described in Section III. Similarly,  $R_{N,3} \approx 2.2 \ \text{k}\Omega$  is found. The achieved  $R_N$ -boosting factor is 9.6×, coinciding with the simulation and evincing the functionality of  $A_{\rm XO-3}$ .

Owing to two reasons, the reduction of  $t_s$  is not commensurate with the  $R_N$ -boosting ratio between  $A_{XO-3}$  and  $A_{XO-1}$ . First, as described in Section III,  $M_{1-3}$  will deviate from their nominal operating points and deteriorate  $R_{N,3}$ . This can be revealed by measuring  $t_s$  against  $t_{sw}$  (Fig. 18). When  $t_{sw}$  is short (<60  $\mu$ s) where M<sub>1-3</sub> are in the subthreshold region, the small-signal model is still valid to estimate  $t_s$  against  $t_{sw}$  [i.e., slope of the curve (~-10) closely matches with  $-R_{N,3}/R_{N,1}$  + 1]. As  $t_{sw}$  further increases, the oscillation drives  $M_{1-3}$  away from its original operating point and worsens  $R_{N,3}$ . Hence, the slope of the curve declines and eventually reaches zero whereas the  $A_{\rm XO-3}$  no longer aids  $t_s$ reduction. Second, the XO entails an overhead time to enter the steady state after switching to  $A_{XO-1}$ . After switching to  $A_{\rm XO-1}$ , the XO still takes ~380  $\mu$ s to enter the steady state. The improvement on  $t_s$  here is limited by the nonideality of the ULV  $A_{XO-3}$ . In fact, for the amplifiers with standard I/O voltage and higher output swing, the reduction of  $t_s$  should be more profound and better matched with the  $R_N$ -boosting ratio.



Fig. 17. Estimated  $R_N$  from the exponential growth of  $X_{OUT}$ 's amplitude (before the transistors enter triode/cutoff region).



Fig. 18. Total  $t_s$  versus  $t_{sw}$ , the enabling time of  $A_{XO-3}$  (without SSCI).

With both  $A_{\rm XO-3}$  and SSCI enabled,  $t_S$  is further shortened to 400  $\mu$ s (3.3× reduction) and the corresponding  $E_S$  is 14.2 nJ (2.8× reduction) [Fig. 16(b)]. When switching from  $A_{\rm XO-3}$  to  $A_{\rm XO-1}$  that have different output impedances and thus operating frequency, there is an instantaneous change of the output swing, since the magnitude of current passing through the crystal does not change abruptly. The percentage of energy consumed in the startup phase by the SSCI,  $A_{\rm XO-3}$ , and  $A_{\rm XO-1}$  is 7%, 39%, and 53%, respectively. It has been verified that  $t_{\rm sw}$  can tolerate ±50% uncertainty for <10%  $t_S$ variation, implying that an adequate  $t_s$  can be obtained even with non-optimal  $t_{\rm sw}$  (e.g., variation on PVT and crystal's parameters). This also justifies that the existed RO will be good enough to control  $t_{\rm sw}$ , avoiding any external detection and control mechanism.

For the transient frequency of the XO, it takes ~300  $\mu$ s to settle for a ±20 ppm  $f_0$  accuracy (i.e., 50 kHz drifting from the center frequency of 2.44 GHz in a packet, as defined in [29]). This result is 3.5× faster than the case without startup aid (Fig. 19). Fig. 20 plots the summary of the reduction in  $t_S$  and  $E_S$  with different startup aids. The steady-state power is 31.8  $\mu$ W at 0.35 V, and the PN is -134 dBc/Hz at 1-kHz offset [Fig. 21(a)], being adequate for most IoT applications and comparable to other state-of-the-art XOs with a standard voltage (e.g., [4], it reports a PN of -136 dBc/Hz at 1 kHz and at  $f_0 = 26$  MHz). As illustrated in Fig. 21(a), the PN of the  $A_{XO-1}$  is 15 dB better than that of  $A_{XO-3}$ , confirming the poorer PN performance of the  $A_{XO-3}$ .

TABLE II Performance Summary and Comparison With Recent Art

_		This	work	JSSC'16 [12]	ISSCO	2'16 [6]	ISSCC'17 [13]	JSSC'18 [14] ¶	
Applications	s BLE		Bluetooth	BLE		BLE	N/A		
Fast-startup	Fast-startup techniques ULV inductive 3-stage g <sub>m</sub> + SSCI		Chirp injection + g <sub>m</sub> -boosting	Dithered injection		Dynamic load + <i>g</i> <sub>m</sub> -boosting	Precisely-timed CFI		
Steady-state techniques		ULV 1-s + resist	stage g <sub>m</sub> ive load	1-stage inverter	с		1-stage g <sub>m</sub> + current-source load		
CMOS process (nm)		65		180	65		90	65	
Active area (mm <sup>2</sup> )		0.023		0.12	0.08		0.072	0.09 (per XO)	
Supply voltage, V <sub>DD</sub> (V)		0.35*		1.5	1.68		1.0	1.0	
Temperature, T <sub>Range</sub> (°C)		-40 to 90		-30 to 125	-40 to 90		-40 to 90	-40 to 85	
C <sub>L</sub> (pF)		6		8 (off-chip)	6	9	10	9	8
Frequency,	f <sub>0</sub> (MHz)	16	24	39.25	24	24	24	50	10
Startup ene	ergy, <i>E</i> s (nJ)	15.8	14.2	349	-		36.7	13.3	12
Startup time	e, <i>t</i> s (µ <b>s</b> )	460	400	158	64	435	200†	2.2	10
∆ts/ts over	T <sub>range</sub>	9.8%	7.5%	7%	±35%	±20%	26.6%	7%	3%
Δf₀/f₀ (ppm)	versus T <sub>Range</sub>	21.9 ◊	14.1 ◊	±5.5	N/A		N/A	N/A	
	versus V <sub>DD</sub>	13.4 §	17.9 §	±0.6 (1.2 to 1.8 V)	N/A		N/A	N/A	
Steady-stat	e power (µW)	31.6	31.8	181	393	693	95	195	45.5

\* Digital & constant-gm bias circuits are at 0.7 V (current budget: 5 µA) to be generated by an on-chip charge pump as [22].

<sup>†</sup> Amplitude >90% and  $\Delta f_0/f_0 < \pm 20$  ppm.  $\diamond @ 0.35$  V. § Across 0.3 to 0.5 V @ 20 °C.

<sup>¶</sup>Only results from similar crystal packages were compared.



Fig. 19. Transient  $f_0$  profiles of the XO ( $V_{DD} = 0.35$  V, T = 20 °C).

In terms of robustness, we confirm that the XO can uphold a steady-state output swing >80% of  $V_{\rm DD}$  for  $V_{\rm DD} = 0.3$ – 0.5 V [Fig. 21(b)]. For the variation of  $t_s$  against  $V_{\rm DD}$ , it is measured <25% from its mean (400  $\mu$ s) for  $V_{\rm DD} = 0.3$ – 0.5 V [Fig. 22(a)]. Only the RO of the SSCI fails to start if  $V_{\rm DD}$  drops down to 0.25 V, but  $A_{\rm XO-3}$  is still in place to aid  $t_s$  reduction. The frequency deviation ( $\Delta f_0/f_0$ ) is 19.7 ppm (17.9 ppm) across 0.25 (0.3 V) to 0.5 V [Fig. 22(b)]. Over -40 °C-90 °C,  $t_s$  variation is <7.5% [Fig. 22(c)], and the  $\Delta f_0/f_0$ is 14.1 ppm [Fig. 22(d)]. Similar results were obtained for a 16-MHz crystal [i.e.,  $\Delta f_0/f_0 = 13.4$  ppm over 0.3–0.5 V,  $\Delta f_0/f_0 = 21.9$  ppm over -40 °C-90 °C, and  $t_s$  variation: 9.8%].

In another test, the XO was powered by a small commercial solar cell  $(1 \times 3.8 \text{ cm}^2)$  in an indoor environment.

Progress of E<sub>s</sub> and t<sub>s</sub> Reduction (V<sub>DD</sub>=0.35V, T=20°C)



Fig. 20. Progress of  $E_S$  and  $t_s$  reduction of the XO ( $f_0 = 24$  MHz) with different startup aids.



Fig. 21. (a) PN of the XO with  $A_{XO-1}$  and  $A_{XO-3}$  as core versus offset frequency ( $f_0 = 24$  MHz). (b) Output voltage swing of the XO against  $V_{DD}$ .

Its nominal output voltage is close to 0.35 V at a solar irradiance of 0.4 mW/cm<sup>2</sup>. Then, the output voltage of the solar cell is swept by altering the light reaching the solar cell.



Fig. 22. Measured XO ( $f_0 = 24$  MHz) performances. (a) Startup time against  $V_{\text{DD}}$ . (b) Frequency stability against  $V_{\text{DD}}$ . (c) Startup time against temperature. (d) Frequency stability against temperature.



Fig. 23. Startup energy of XOs from the literature versus their core  $V_{DD}$ . Some of their  $E_S$  values (marked with #) were not reported, thus they are estimated through the multiplication of their startup times by the steady-state powers.

The measured metrics of the XO powered by the solar cell are comparable to those using a typical power supply [Fig. 22(a) and (b)].

Table II and Fig. 23 benchmark the performance of the XO with the prior art. In terms of  $E_s$ , this paper is >2.6× better than [13] and slightly higher than [14]. Furthermore, the proposed circuit can be considered in the vanguard, since it proves the feasibility of regulation-free operation under a wide range of sub-0.5-V  $V_{\text{DD}}$ , while conforming to the frequency-stability specification of the BLE standard.

## V. CONCLUSION

A regulation-free sub-0.5-V XO for energy-harvesting BLE radios has been reported. Two circuit techniques, dual-mode  $g_m$  and SSCI, are introduced to reduce the startup time  $t_s$  and energy  $E_s$ . The dual-mode  $g_m$  exploits the inductive feature of a three-stage  $g_m$  ( $A_{XO-3}$ ) to counteract  $C_S$  of the crystal during the startup, and the low-noise feature of a

one-stage  $g_m$  ( $A_{XO-1}$ ) to preserve the PN in the steady state. Both  $A_{XO-1}$  and  $A_{XO-3}$  are ULV-enabled using resistive-load CS amplifiers. For the SSCI, a scalable chirping sequence effectively raises the initial oscillation amplitude of the crystal under different conditions, avoiding the need of a precisely trimmed AO. The XO prototyped in 65-nm CMOS has a compact area (0.023 mm<sup>2</sup>) that is > 3.1× smaller than the prior art. The measured  $t_s$  and  $E_s$  of the XO, with a 24-MHz crystal, are 400  $\mu$ s and 14.2 nJ, respectively. The frequency stability against voltage (0.3–0.5 V) is 17.9 ppm and temperature (-40 °C-90 °C) is 14.1 ppm; both conform to the BLE standard.

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